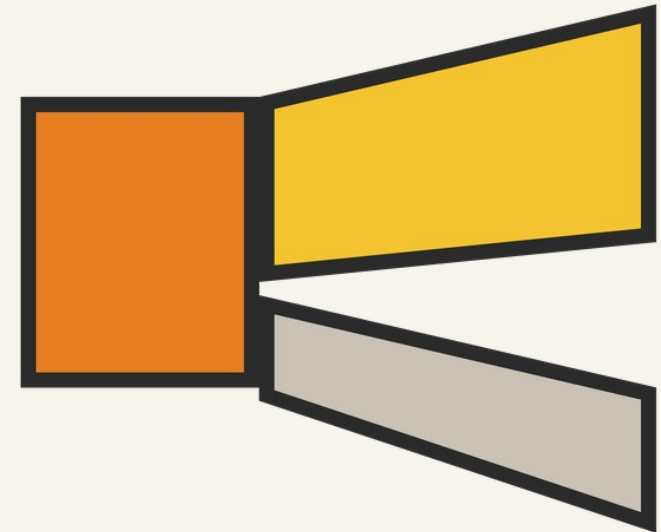


Efficiency

How much of what goes in actually does the job?



LEARNING INTENTION

To calculate efficiency as a ratio and as a percentage, for both energy and power.

Daily Review

SHOW ME BOARDS

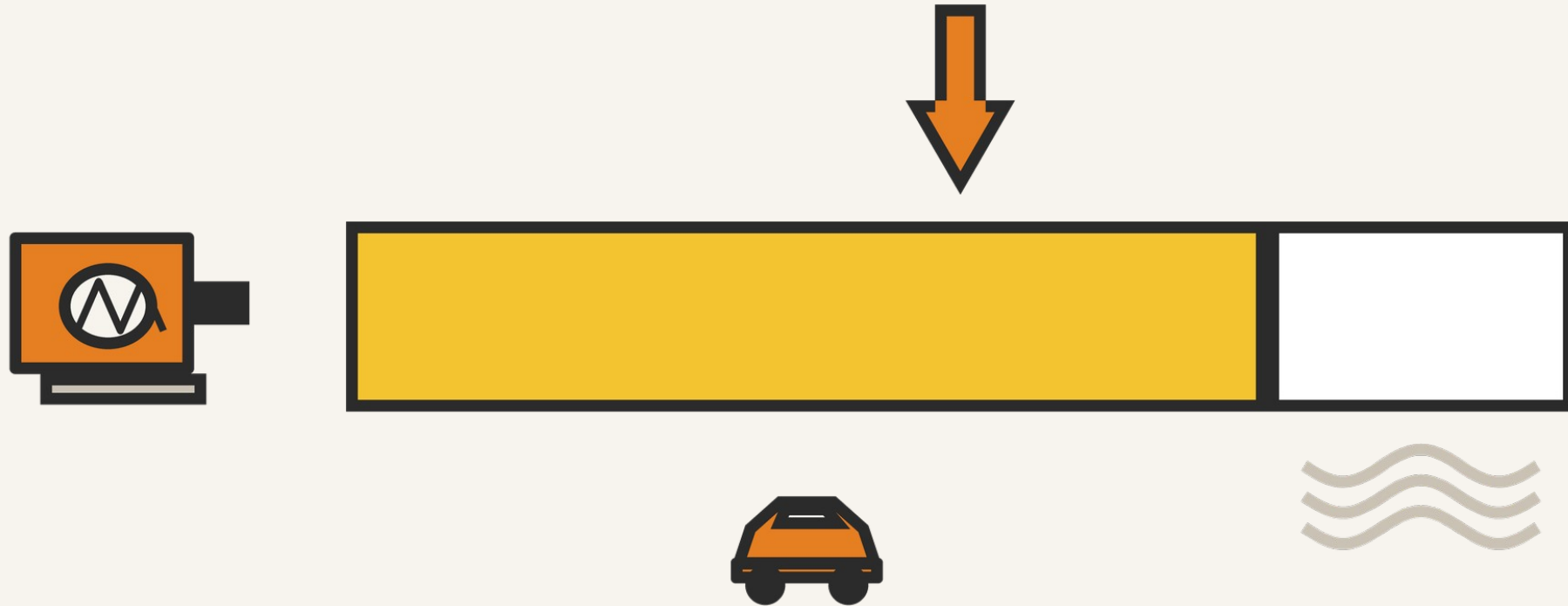
- 1 Write the formula for power.
- 2 A motor transfers 8 000 J in 20 s. Calculate the power.
- 3 Change 2 kW into watts.
- 4 State the law of conservation of energy.
- 5 A system takes in 700 J and wastes 100 J. How much is useful?

By the end of this lesson...

- 1 I can calculate the wasted energy from the input and the useful output.
- 2 I can state $\eta = E_{\text{out}} \div E_{\text{in}}$ and use it as a ratio.
- 3 I can calculate a percentage efficiency.
- 4 I can use the same formula with power values.
- 5 I can explain why no real system reaches 100 %.

Account for Every Joule

Some of the input does the job. The rest is wasted, usually as heat or sound.



the whole bar is the input · the yellow part is useful · the rest is wasted

Task 1 – Account for the Energy

Five systems. Work out the wasted energy in each.
Wasted = input – useful. Nothing more complicated than that.

Check every row: your three numbers must add up.

Booklet – “TASK: Account for the Energy”

Efficiency

Efficiency compares the useful output with the total input.

$$\eta = (E_{\text{out}} \div E_{\text{in}}) \times 100$$

η

efficiency (%)

E_{out}

useful output energy (J)

E_{in}

input energy (J)

Without the $\times 100$ you get a ratio. The same formula works with power: $\eta = P_{\text{out}} \div P_{\text{in}}$.

Worked Example – Motor

An electric motor is supplied with 800 J of energy.
It produces 600 J of useful kinetic energy. Calculate the efficiency.

$$E_{\text{out}} = 600 \text{ J}$$

$$E_{\text{in}} = 800 \text{ J}$$

$$\eta = ?$$

$$\eta = (E_{\text{out}} \div E_{\text{in}}) \times 100$$

$$\eta = (600 \div 800) \times 100$$

$$\underline{\eta = 75 \%}$$

Watch Out – Over 100 %?

THE MISTAKE

- “ $800 \div 600 \times 100 = 133 \%$ ”
- “The answer is 0.75, so I will write 0.75 %.”
- “A really good motor could reach 105 %.”

THE CORRECT ANSWER

- Useful on top, input underneath. Always that way round.
- 0.75 is the ratio. $\times 100$ makes it 75 %.
- Impossible. The useful output is part of the input.

Show Me – Efficiency Basics

SHOW ME BOARDS

- 1 Which number goes on top – the useful output, or the input?
- 2 What is the unit of a percentage efficiency?
- 3 What is the highest efficiency any real system can reach?
- 4 Input 100 J, useful 40 J – what is the efficiency?
- 5 Why can no real system reach 100 %?

Show Me — Basics Again

SHOW ME BOARDS

EXTRA PRACTICE

- 1 What does η stand for?
- 2 What must you multiply by to turn a ratio into a percentage?
- 3 Input 200 J, useful 50 J — what is the efficiency?
- 4 A system is 100 % efficient. What is wrong with that claim?
- 5 Name the two forms wasted energy usually takes.

Show Me – Efficiency Calculations

SHOW ME BOARDS

- 1 Input 400 J, useful 300 J – calculate the percentage efficiency.
- 2 Input 500 W, useful 400 W – calculate the percentage efficiency.
- 3 Input 2 000 J, useful 1 500 J – calculate the percentage efficiency.
- 4 Input 250 W, useful 200 W – calculate the percentage efficiency.
- 5 Input 80 J, useful 20 J – calculate the percentage efficiency.

Show Me – More Calculations

SHOW ME BOARDS

EXTRA PRACTICE

- 1 Input 600 J, useful 540 J – calculate the percentage efficiency.
- 2 Input 1 000 W, useful 250 W – calculate the percentage efficiency.
- 3 Input 50 J, useful 45 J – calculate the percentage efficiency.
- 4 Input 3 000 J, useful 1 800 J – calculate the percentage efficiency.
- 5 Input 900 W, useful 720 W – calculate the percentage efficiency.

Task 2 – Efficiency

Three calculations in your jotter, SQA layout every time.
Q2 is in watts and Q3 is in kilowatts – the formula does not care.

3 marks each. The % sign is part of the answer.

Booklet – “TRY THIS: Efficiency”

Checkpoint

- 1 Write the formula for percentage efficiency.
- 2 Input 1 200 J, useful 900 J – calculate the percentage efficiency.
- 3 What + why: a motor is 75 % efficient. Where is the other 25 %?

Exam Practice — Past Papers

2021 Q10(b)(ii) — output energy from $\eta = 0.72$ (3)

2022 Q14(d) — input power from $\eta = 0.85$ (3)

SQP Q11(b) — $E_{\text{out}} = E_{\text{in}} \times \eta$, rearranged (3)

SQP Q17(b)(iii) — explain why less than 100 % (2)

2025 Q10(d) — E_k from η , then explain (5)

Find the relationship in the data booklet

LOOKING AHEAD

Energy Audits

An energy audit puts the whole picture in one diagram.

Plenary – Prove Your I Can... Statements

SHOW ME BOARDS

- 1 Write the formula for percentage efficiency.
- 2 Input 500 J, useful 250 J – calculate the efficiency.
- 3 Input 60 W, useful 48 W – calculate the efficiency.
- 4 What is the highest efficiency a real system can reach?
- 5 Where does the wasted energy usually end up?

Plenary – More Quick Checks

SHOW ME BOARDS

EXTRA PRACTICE

- 1 What does E_{out} stand for?
- 2 Input 200 J, useful 160 J – calculate the efficiency.
- 3 Turn a ratio of 0.45 into a percentage.
- 4 Input 40 W, useful 10 W – calculate the efficiency.
- 5 Why is efficiency never given a unit like joules?

Extension — If You Finish Early

- 1 A system is 30 % efficient and takes in 900 J. Find the useful output.
- 2 A pump is 80 % efficient and gives 400 J useful. Find the input energy.
- 3 What + why: which wastes more energy — a 90 % motor using 1 000 J, or a 40 % lamp using 100 J?

Extension — More Challenges

EXTRA PRACTICE

1

A system is 25 % efficient and takes in 480 J. Find the useful output.

2

A motor is 60 % efficient and wastes 800 J. Find the input energy.

3

What + why: why do engineers quote efficiency as a percentage rather than in joules?